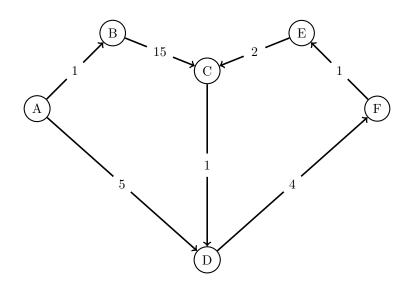
1 The Shortest Path To Your Heart

For the graph below, let g(u, v) be the weight of the edge between any nodes u and v. Let h(u, v) be the value returned by the heuristic for any nodes u and v.



Below, the pseudocode for Dijkstra's and A^{*} are both shown for your reference throughout the problem.

A* Pseudocode

Dijkstra's Pseudocode

```
PQ = new PriorityQueue()
    PQ = new PriorityQueue()
1
    PQ.add(A, 0)
                                                             PQ.add(A, h(A, goal))
2
                                                         2
    PQ.add(v, infinity) # (all nodes except A).
                                                             PQ.add(v, infinity) # (all nodes except A).
3
                                                         3
4
                                                         4
                                                             distTo = {} # map
    distTo = {} # map
5
                                                         5
    edgeTo = {} # map
                                                             distTo[A] = 0
6
                                                         6
    distTo[A] = 0
                                                             distTo[v] = infinity # (all nodes except A).
7
                                                         7
    distTo[v] = infinity # (all nodes except A).
8
                                                         8
                                                             while (not PQ.isEmpty()):
9
                                                         9
    while (not PQ.isEmpty()):
                                                               poppedNode, poppedPriority = PQ.pop()
10
                                                         10
      poppedNode, poppedPriority = PQ.pop()
                                                               if (poppedNode == goal): terminate
11
                                                         11
12
                                                         12
      for child in poppedNode.children:
                                                                  for child in poppedNode.children:
13
                                                         13
        potentialDist = distTo[poppedNode] +
                                                                    potentialDist = distTo[poppedNode] +
                                                         14
14
             edgeWeight(poppedNode, child)
                                                                        edgeWeight(poppedNode, child)
15
                                                         15
                                                         16
16
        if potentialDist < distTo[child]:</pre>
                                                                    if potentialDist < distTo[child]:</pre>
                                                         17
17
          distTo.put(child, potentialDist)
                                                                      distTo.put(child, potentialDist)
18
                                                         18
                                                                      PQ.changePriority(child, potentialDist + h(child, goal))
          PQ.changePriority(child, potentialDist)
                                                         19
19
          edgeTo[child] = poppedNode
                                                                      edgeTo[child] = poppedNode
20
                                                         20
```

2 Shortest Paths, MSTs

(a) Run Dijkstra's algorithm to find the shortest paths from A to every other vertex. You may find it helpful to keep track of the priority queue. We have provided a table to keep track of best distances, and the adjacent vertex that has an edge going to the target vertex in the current shortest paths tree so far.

	A	В	C	D	E	F
DistTo						
EdgeTo						

(b) Given the weights and heuristic values for the graph above, what path would A^* search return, starting from A and with F as a goal?

	. 0
Edge weights	Heuristics
g(A,B) = 1	h(A,F) = 8
g(A,D) = 5	h(B,F) = 16
g(B,C) = 15	h(C,F) = 4
g(C,D)=1	h(D,F) = 4
g(D,F)=4	h(E,F) = 5
g(F, E) = 1	
g(E,C)=2	

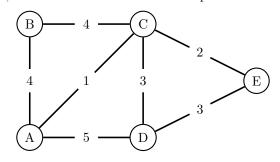
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	A	В	С	D	E	F
DistTo						
EdgeTo						

(c) Based on the heuristics for part b, is the A* heuristic for this graph good? In other words, will it always give us the actual shortest path from A to F? If it is good, give an example of a change you would make to the heuristic so that it is no longer good. If it is not, correct it.

2 Minimalist Moles

Circle the mole wants to dig a network of tunnels connecting all of his secret hideouts. There are a few set paths between the secret hideouts that Circle can choose to possibly include in his tunnel system, shown below. However, some portions of the ground are harder to dig than others, and Circle wants to do as little work as possible. In the diagram below, the numbers next to the paths correspond to how hard that path is to dig for Circle. Lucky for us, he knows how to use MSTs to optimize the tunnel paths!



Below, the pseudocode for Kruskal's and Prim's are shown for your reference throughout the problem.

Prim's Pseudocode

		1 2	Start with any node. Add that node to the set of nodes in the MST.
1	while there are still nodes not in the MST:	3	While there are still nodes not in the MST:
2	Add the lightest edge	4	Add the lightest edge from a node in the MST
3	that does not create a cycle.	5	that leads to a new node that is unvisited.
4	Add the new node to the	6	Add the new node to the set of
5	set of nodes in the MST.	7	nodes in the MST.

(a) Find a valid MST for the graph above using Kruskal's algorithm, then Prim's. For Prim's algorithm, take A as the start node. In both cases, if there is ever a tie, choose the edge that connects two nodes with lower alphabetical order.

(b) Are the above MSTs different or the same? If different, describe a tie-breaking scheme that would make them the same. If the same, describe a tie-breaking scheme that would make them different.

3 Sticky Flights

Your airline company has been contracted to fly a large shipment of honey from Honeysville to the 61Bees in Apēs City. However, the airplane doesn't have enough fuel capacity to fly directly to Apēs City so it will stop at at least one of n airports along the way to refuel. Refueling takes an hour, and if the airport is one of k < n airports, your airplane will be grounded for six hours due to curfews (refueling is included in the six hours). The 61Bees want their honey as soon as possible so please design an algorithm to find the route that will allow your airplane to reach Apēs City in the least amount of hours.

Hint: Think of the n airports as a graph, where the paths between them are edges of weight equivalent to the number of hours it takes to fly from airport A to airport B. You may assume that the amount of time it takes to fly from A to B is equal to the amount of time it takes to fly from B to A.